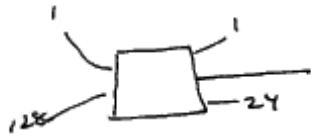


Solutions to Network Performance Homework EECS 663



1. $C = 64 \text{ kb/s}$
 $L = 128 \text{ bytes} = 1024 \text{ bits}$

$$\bar{T}_h = \frac{1024}{64 \times 10^3} = 16 \text{ ms}$$

$P_L = 1\%$ $N = 24 = \# \text{ output lines}$

From table
 $A = 15.3 = \lambda \bar{T}_h$

$$\lambda = 15.3 / 0.016 = 956 \text{ packets/sec}$$

$M = 128 = \text{Input lines}$

$$\lambda_i = 956 / 128 = 7.4 \text{ packets/sec}$$

2.

$M = 24$ $\lambda_i = 10 \text{ packets/sec}$

$$\lambda_T = 24 \cdot 10 = 240 \text{ packets/sec}$$

$L = 100 \text{ bytes} = 800 \text{ bits}$

$C = 56 \text{ kb/s}$

$$\bar{T}_h = 800 / 56,000 = 14 \text{ ms}$$

$B = 20^{10}$

$A = 240 \cdot 0.014 = 3.4 \Rightarrow N = 5 \text{ from table}$

3. $P_B = 1\%$ $M = 120$ phones
 .05 Erlang / phone
 $A = .05 \cdot 120 = 6$ Erlangs
 from table $N = 13$

Traffic 6 \rightarrow 9 Erlangs
 $N = 13 \rightarrow \sim 6\%$ from table

4.

$$\bar{L} = 125 \text{ bytes} = 1000 \text{ bits}$$

$$\lambda_i = 10 \text{ packets/sec}$$

$$M = 25 \text{ terminals}$$

$$\lambda_T = 250 \text{ packets/sec}$$

Design start mux such that

$$E\{T\} = 100 \text{ms}$$

$$0.1 = \frac{1}{\mu - \lambda_T} = E\{T\}$$

$$10 = \mu - \lambda_T \Rightarrow \mu = 260 \text{ packets/sec}$$

$$C = (1000 \text{ bits/packet}) 260 \text{ packets/sec}$$

$$= 260 \text{ kb/s}$$

5. Design start with

$$P_B < 2 \times 10^{-4}$$

$$E\{T\} < 512 \text{ ms}$$

given

$$\lambda = 10 \text{ packets/sec}$$

$$L = 1024 \text{ bits/packet}$$

$$.512 = \frac{1}{\mu - \lambda} = E\{T\}$$

$$1.95 = \mu - \lambda \rightarrow \mu = 11.95$$

$$\rightarrow C = 12,236 \text{ b/s}$$

now use $\rho = \lambda / \mu = 10 / 11.95 = .84$

$$P_0 = \frac{(1-\rho)\rho^N}{1-\rho^{N+1}} \rightarrow N = 41 \text{ so}$$

$$M/M/1/N \quad \text{buffer size} = 40$$

6. $M = 50$ VBR sources

$$L = 2000 \text{ b.its}$$

$$\lambda_i = 1000 \text{ packets/sec}$$

$$C = 150 \text{ Mb/s}$$

$$\lambda_T = 50,000 \text{ packets/sec}$$

$$\rho = \frac{(2 \times 10^3 \text{ bits/packet}) 50,000 \text{ packets/sec}}{150 \times 10^6 \text{ b/s}}$$

$$= .667$$

$$E\{N\} = \frac{\rho}{1-\rho} = 2$$

$$E\{T\} = E\{N\} / \lambda_T = 40 \mu\text{s}$$