

1

1. Given a system $y(t) = tx(t) + 3$

6 pts each

- a. Is the system linear or nonlinear? Circle LINEAR or NONLINEAR and justify.
- b. Is the system time invariant or time varying? Circle TIME INVARIANT or TIME VARYING and justify.
- c. Is the system dynamic (with memory) or static (memory-less)? Circle DYNAMIC or STATIC and justify.

- a. Non-linear
- b. time varying
- c. static

2. Given $z(t)=10\cos(5t)$,

$$x(t) = 10 \cos(5t) + 20\cos(10t), \text{ and}$$
$$y(t) = 10 \operatorname{rect}\left(\frac{t-1}{4}\right).$$

- a. 4 pts What is the period of $z(t)$?
- b. 3 pts Find the energy in $x(t)$.
- c. 3 pts Find the power in $x(t)$.
- d. 3 pts Is $x(t)$ an energy or power signal?
- e. 3 pts Find the energy in $y(t)$.
- f. 3 pts Find the power in $y(t)$.
- g. 3 pts Is $y(t)$ an energy or power signal?

a.

$$\frac{2\pi}{5}$$

Out[$\#$]=

$$1.25664$$

b. $E_x=\infty$

c. & d 250 Power signal

$$\frac{10^2}{2} + \frac{20^2}{2}$$

Out[$\#$]=

$$250$$

e.

$$\int_{-\infty}^{\infty} \left(10 * \operatorname{UnitBox}\left[\frac{t-1}{4}\right]\right)^2 dt$$

Out[$\#$]=

$$400$$

f. $P_y=0$ g. Energy signal

3. Given a LTI system has an impulse response $h(t) = r(t)\text{rect}(\frac{t-2}{2})$.

6 pts each

a. Find and sketch the system output for an input of $\delta(t)$.

b. Is the system causal? Circle YES or NO and justify your answer.

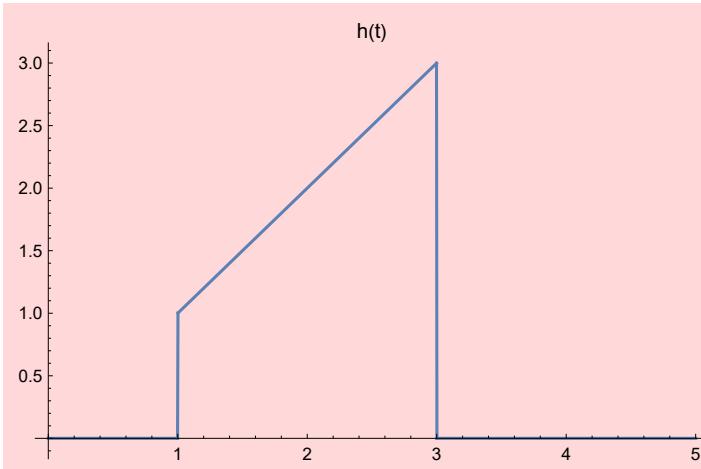
c. Is the system BIBO stable? Circle YES or NO and justify your answer.

For an input signal $x(t) = 10 \text{ rect}(\frac{t-4}{4})$

d. Find the system output at $t=2$, i.e., $y(2)$.

e. Find the system output at $t=4$, i.e., $y(4)$.

Out[$\#$] =



b. Causal

c. Stable

In[$\#$] =

$y3[2]$

$y3[4]$

Out[$\#$] =

0

Out[$\#$] =

15

4. LTI system is described by a the linear, constant-coefficient, differential equation

$$\frac{1}{4} \frac{dy(t)}{dt} + y(t) = x(t)$$

15 pts each

a. Find $H(\omega)$.

b. Given $x(t) = 1+2\cos(t) + 4\cos(4t)$ find the system output $y(t)$

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In[6]:= H[w_] = 1/(I*w/4 + 1)
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Out[6]=

$$\frac{1}{1 + \frac{i w}{4}}$$

Out[6]=

$$\frac{1}{1 + \frac{w^2}{16}}$$

Out[6]=

$$-\text{ArcTan}\left[\frac{w}{4}\right]$$

$$H[0] * 1 + 2 * \text{absH4}[1.] * \text{Cos}[t + \text{angH4}[1.]] + 4. * \text{absH4}[4.] * \text{Cos}[4 * t + \text{angH4}[4.]]$$

Out[6]=

$$1 + 2.82843 \text{Cos}[0.785398 - 4 t] + 1.94029 \text{Cos}[0.244979 - t]$$

$$|$$

$$\int x^n \sin(x) dx = -x^n \cos(x) + n \int x^{n-1} \cos(x) dx$$

$$\int x^n \cos(x) dx = x^n \sin(x) - n \int x^{n-1} \sin(x) dx$$

$$\cos(x)\cos(y) = \frac{1}{2}[\cos(x-y) + \cos(x+y)]$$

$$\int x^n e^{ax} dx = \frac{e^{ax}}{a^{n+1}} [(ax)^n - n(ax)^{n-1} + n(n-1)(ax)^{n-2} + \dots + (-1)^{n-1} n!(ax) + (-1)^n n!], \quad n \geq 0$$

$$\sin(x)\sin(y) = \frac{1}{2}[\cos(x-y) - \cos(x+y)]$$

$$\int e^{ax} \sin(bx) dx = \frac{e^{ax}}{a^2 + b^2} [a \sin(bx) - b \cos(bx)]$$

$$\sin(x)\cos(y) = \frac{1}{2}[\sin(x-y) + \sin(x+y)]$$

$$\int e^{ax} \cos(bx) dx = \frac{e^{ax}}{a^2 + b^2} [a \cos(bx) + b \sin(bx)]$$

$$\cos(x+y) = \cos(x)\cos(y) - \sin(x)\sin(y)$$

$$\int \frac{dx}{(x^2 \pm a^2)^{\frac{1}{2}}} = \ln \left| x + (x^2 \pm a^2)^{\frac{1}{2}} \right|$$

$$\sin(x+y) = \sin(x)\cos(y) + \cos(x)\sin(y)$$

$$\int_0^\infty \frac{\sin(mx)}{x} dx = \begin{cases} \pi/2, & m > 0 \\ 0, & m = 0 \\ -\pi/2, & m < 0 \end{cases} = \frac{\pi}{2} \operatorname{sgn}(m)$$

$$\frac{d}{dx} [\tan^{-1}(x)] = \frac{1}{1+x^2}$$

$$|Z|^2 = ZZ^*$$

$$\sum_{n=0}^{N-1} r^n = \begin{cases} \frac{1-r^N}{1-r}, & r \neq 1 \\ N, & r = 1 \end{cases}$$

$$\sum_{n=0}^{\infty} r^n = \frac{1}{1-r}, \quad |r| < 1$$

$$\sum_{n=k}^{\infty} r^n = \frac{r^k}{1-r}, \quad |r| < 1$$

$$\sum_{n=0}^{\infty} nr^n = \frac{r}{(1-r)^2}, \quad |r| < 1$$