

EECS 861
Topics for Test 2
Fall 2024

Power Spectral Density, $S_x(f)$

- $E[X(t)]$
- $\text{Var}[X(t)]$
- Bandwidth and correlation time

$$\text{Bandwidth- } B_e = \frac{1}{2} \frac{R_{xx}(0)}{S_x(0)}$$

- % In-band power
- Random sequences

Properties of time averages- Integration of $X(t)$

- $E[\text{Time Average}]$
- $\text{Var}[\text{Time Average}]$

Independent Increments – Point Processes – Poisson Process

Variance of time averages

- For large $2B_eT$, Number of uncorrelated samples in $T(\text{sec}) \sim 2B_eT$

Ergodicity

Decomposition of RPs

Sampling of random processes

Quantizing

Major classes of RP

- Bandlimited White Noise
- ARMA, output = $Y[n]$
 - $E[Y[n]]$
 - $\text{Var}[Y[n]]$
 - $R_{YY}[k]$

Response of Systems to Random Inputs

- Discrete time systems
- Continuous time systems
- Output power spectral density
- Output autocorrelation functions
- Output S/N

Detection

- MAP rule
- Detector performance, $P_{\text{false alarm}}$, P_{Hit} , P_{miss} , P_{error}
- Bayes detection with cost
- Neyman-Pearson rule
- ROC