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The 90° Hybrid Coupler

The 90° Hybrid Coupler, otherwise known as the **Quadrature Coupler**, has the **same** form as the directional coupler:



However, for **this** coupler we find that

Therefore, the scattering matrix of a quadrature coupler is:

 $\alpha = \beta = \frac{1}{\sqrt{2}}$



It is evident that, just as with the directional coupler, the ports are **matched** and the device is **lossless**. Note also, that if a signal is incident on one port only, then there will be a port from which **no** power will exit (i.e., an **isolation** port). Unlike the directional coupler, the power that is flows into the input port will be **evenly** divided between the two non-isolated ports.

For example, if 10 mW is incident on port 3 (and all other ports are matched), then 5 mW will flow out of **both** port 1 and port 4, while no power will exit port 2 (the isolated port).

Note however, that the although the **magnitudes** of the signals leaving ports 1 and 4 are **equal**, the relative **phase** of the two signals are separated by **90 degrees** ($e^{j\frac{\pi}{2}} = j$).

We find, therefore, that if in real terms the voltage out of port 1 is:

$$\mathbf{V}_{1}(\mathbf{z}, \mathbf{t}) = |\mathbf{V}_{1}^{-}|\cos(\mathbf{w}\mathbf{t} + \beta\mathbf{z})$$

then the signal form port 4 will be:

$$\mathbf{v}_{4}(\mathbf{z},\mathbf{t}) = |\mathbf{v}_{4}^{-}| \operatorname{sin}(\mathbf{w}\mathbf{t} + \beta \mathbf{z})$$

There are **many** useful applications where we require both the **sine** and **cosine** of a signal!

